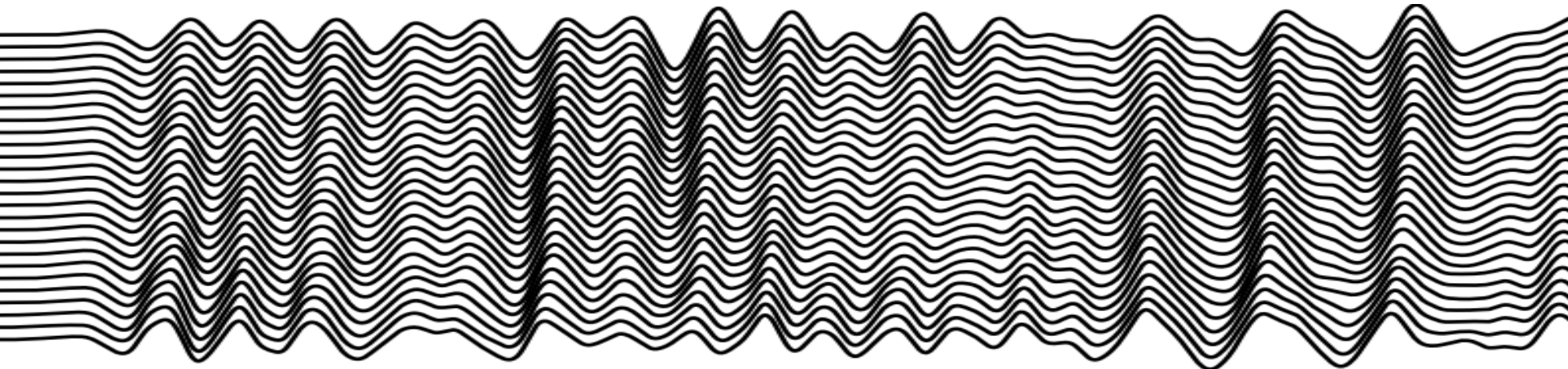


What's that wiggle?



The challenges (and solutions) of using fibre-optic cables as seismological antennas



UNIVERSITÉ
CÔTE D'AZUR 

3iA Côte d'Azur

Institut interdisciplinaire
d'intelligence artificielle

van den Ende & Ampuero
(2021), *Evaluating seismic
beamforming capabilities of
distributed acoustic sensing
arrays*, Solid Earth 12

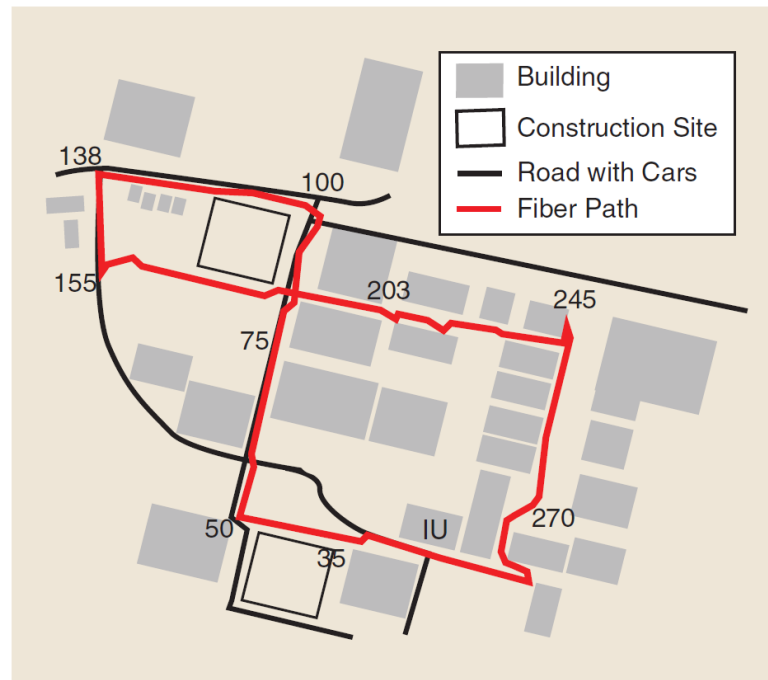
DAS arrays are the future (?)

Glacier

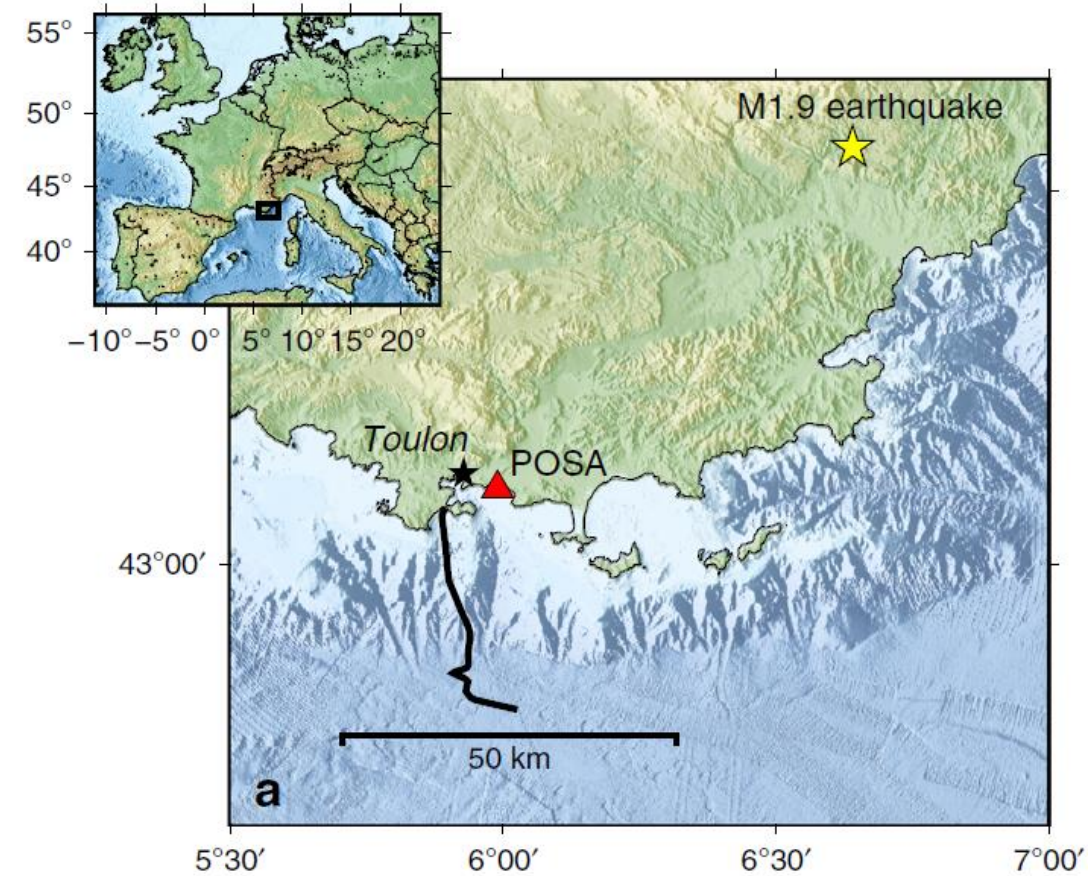
Walter et al. (2020)



Stanford Campus
Martin et al. (2018)

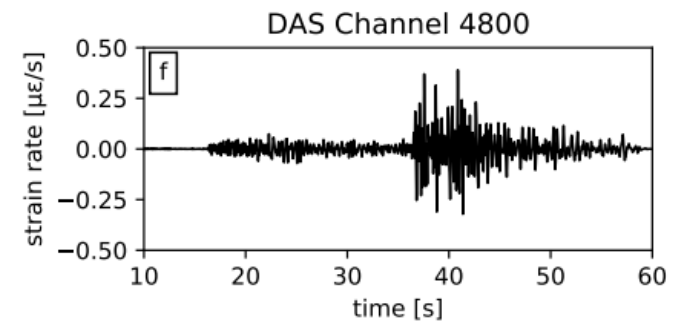
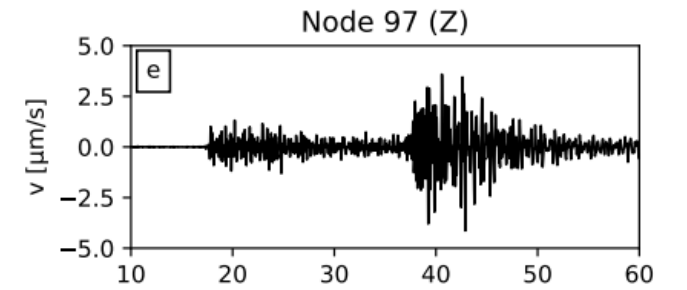
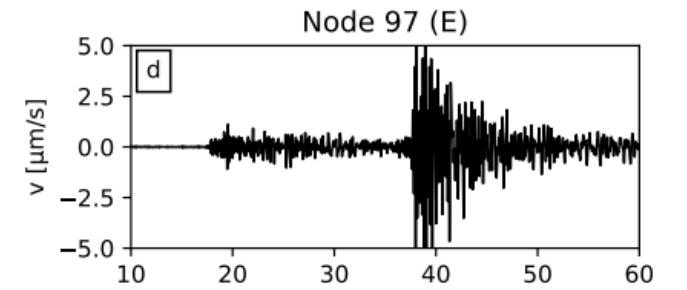
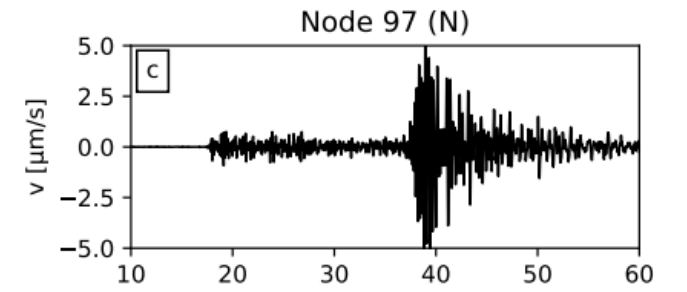
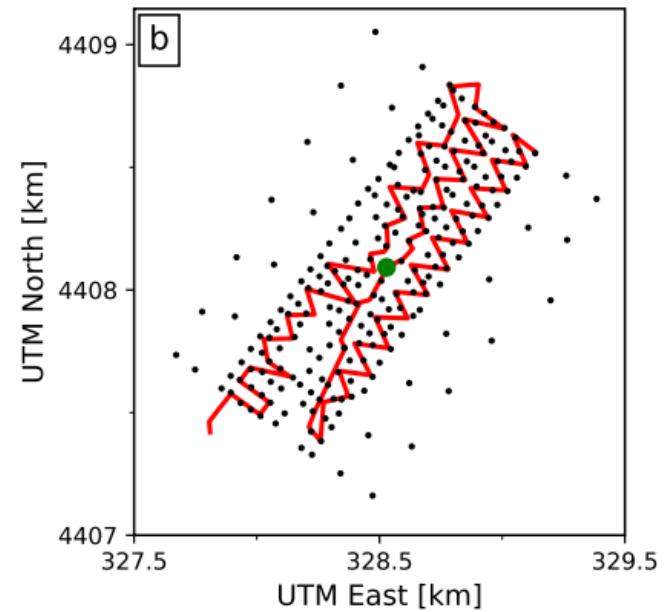
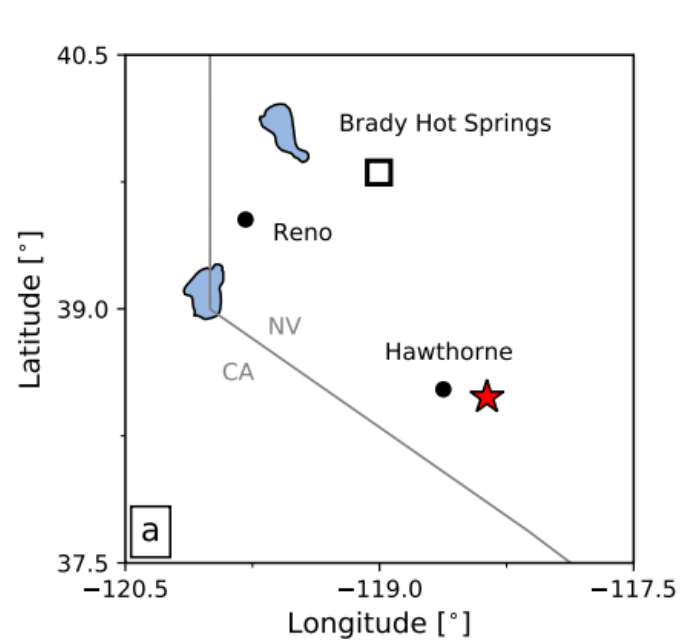
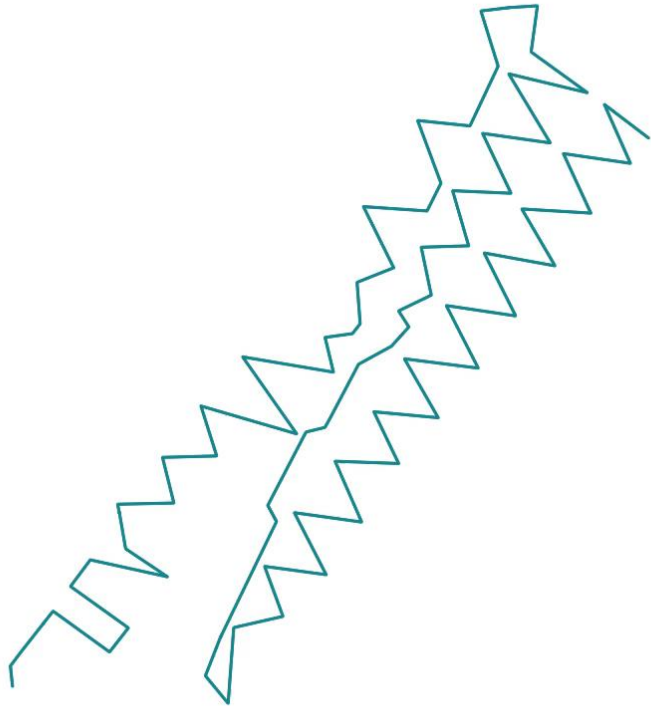


Offshore telecommunication cable
Sladen et al. (2019)



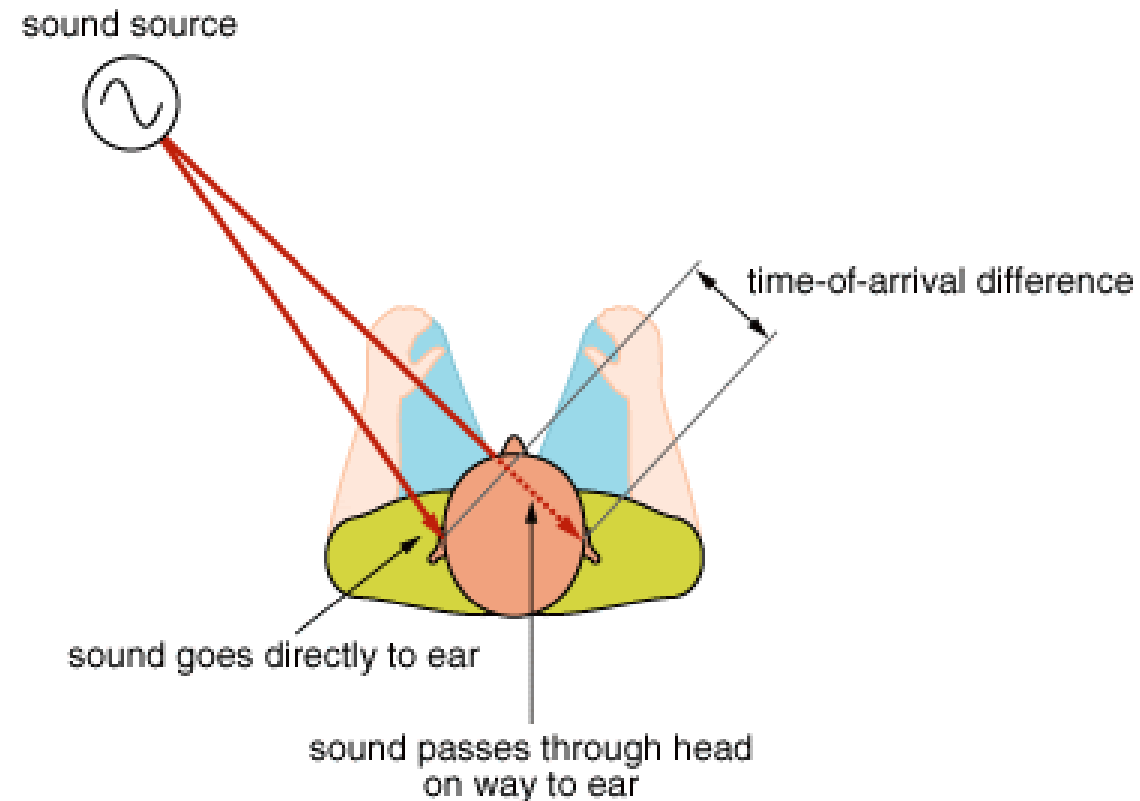
Hawthorne M4.3 earthquake

See: Feigle & the PoroTomo team (2018)
Wang et al. (2018)

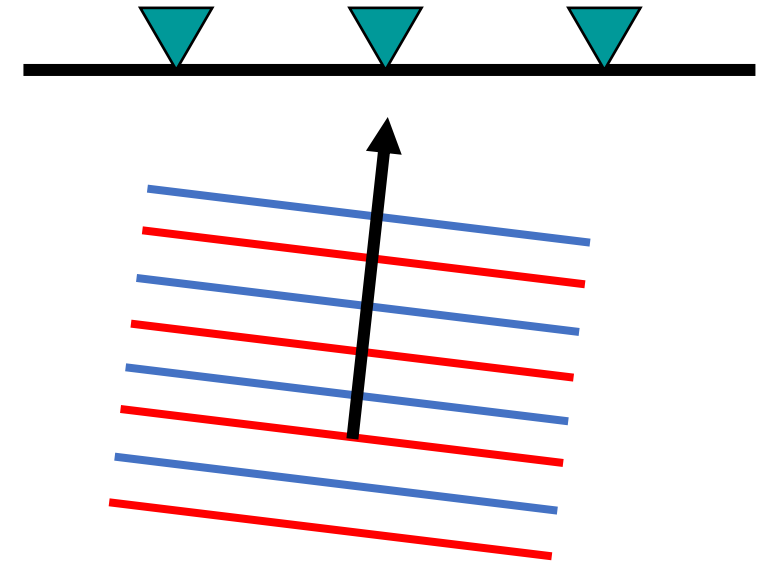
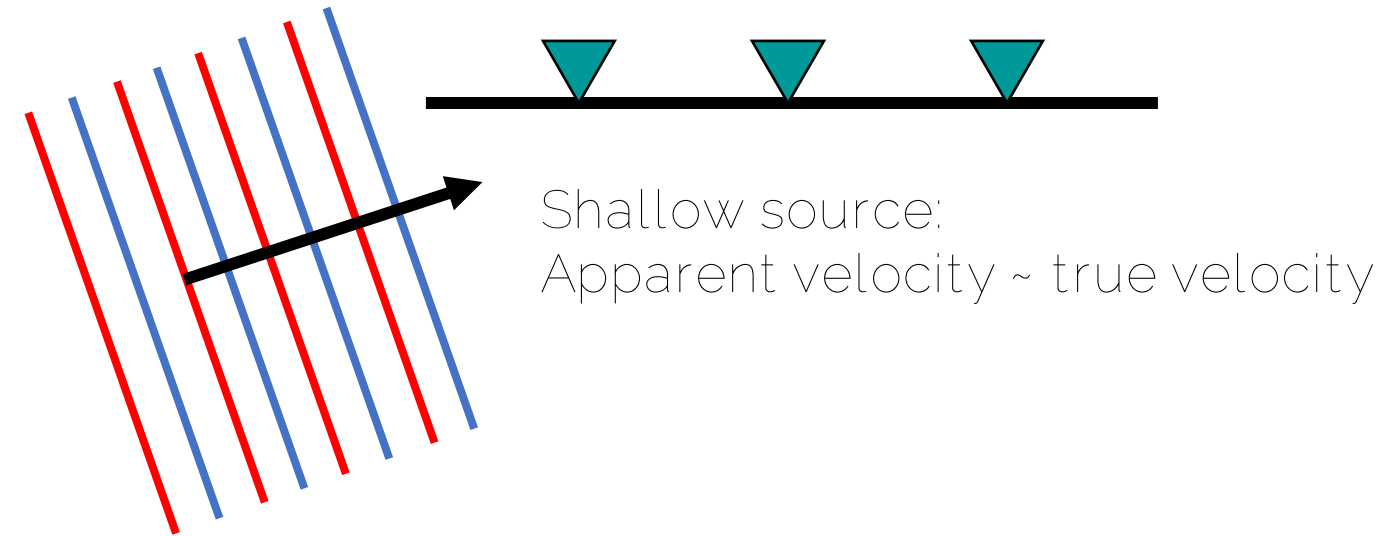


Quick primer on beamforming

- Arrival time of signals depends on source-receiver distance
- Array of sensors (your ears): time delay caused by offset between sensors, dependent on azimuth
- **Beamforming: use sensor array to estimate direction-of-arrival and apparent phase velocity**
- Frequency-domain **MU**ltiple **SI**gnal **C**lassification (MUSIC) beamforming



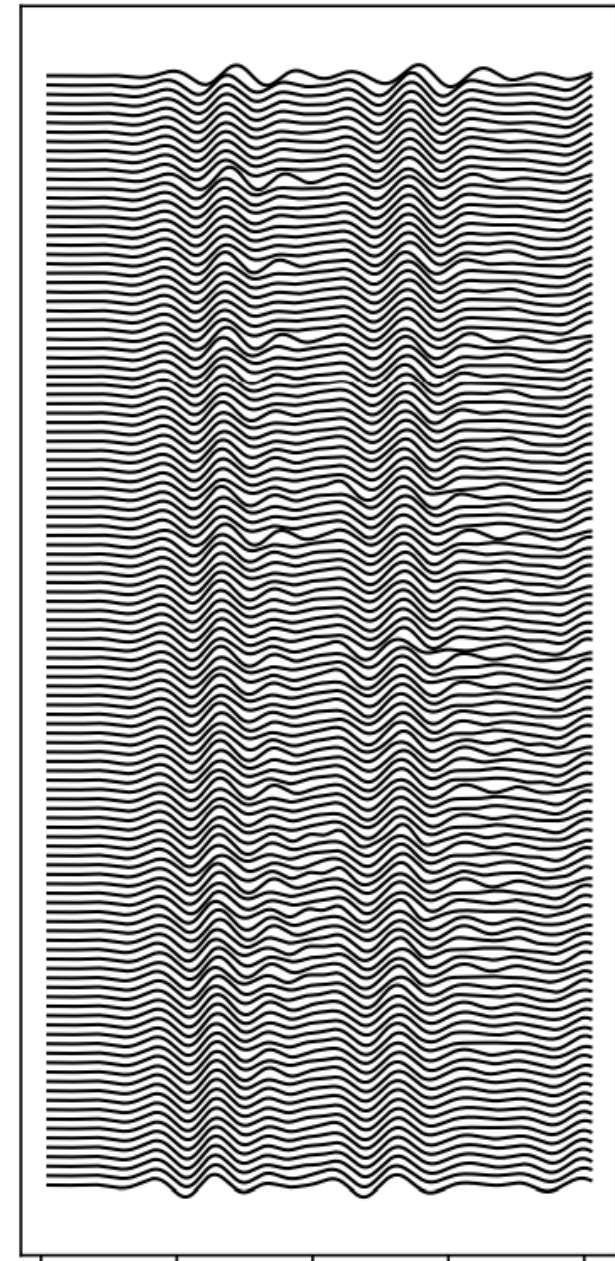
Quick primer on beamforming



Deep/distant source:
Apparent velocity \gg true velocity

Z-component

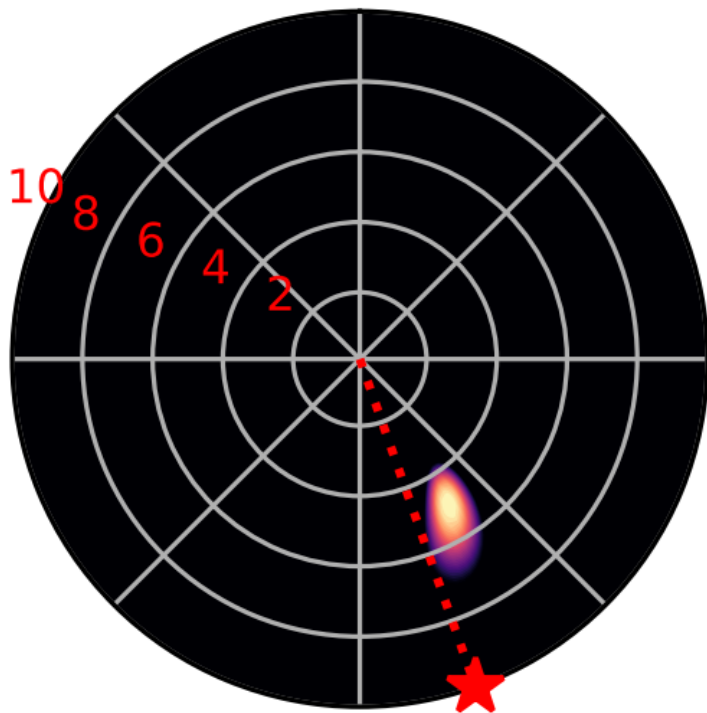
Nodal seismometer beamforming



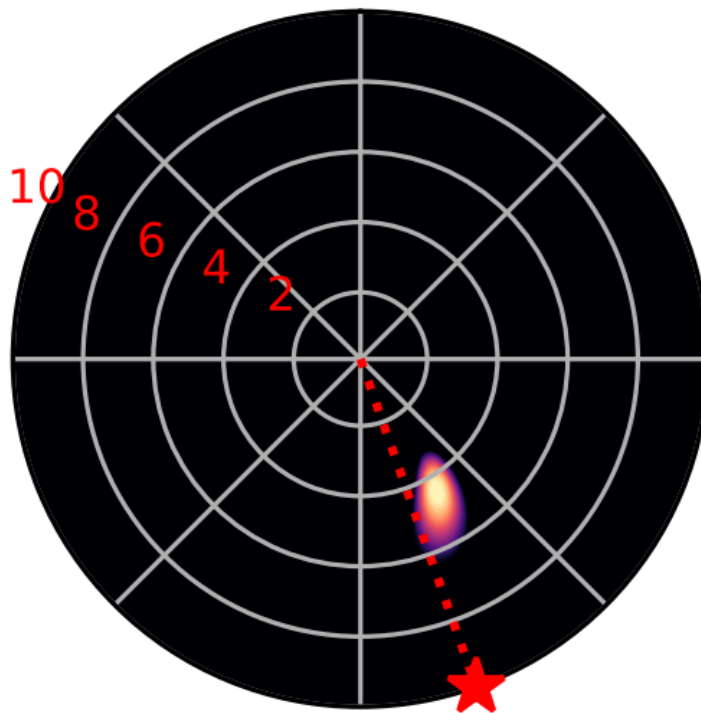
15.0 17.5 20.0 22.5 25.0
time [s]

Nodal seismometer beamforming

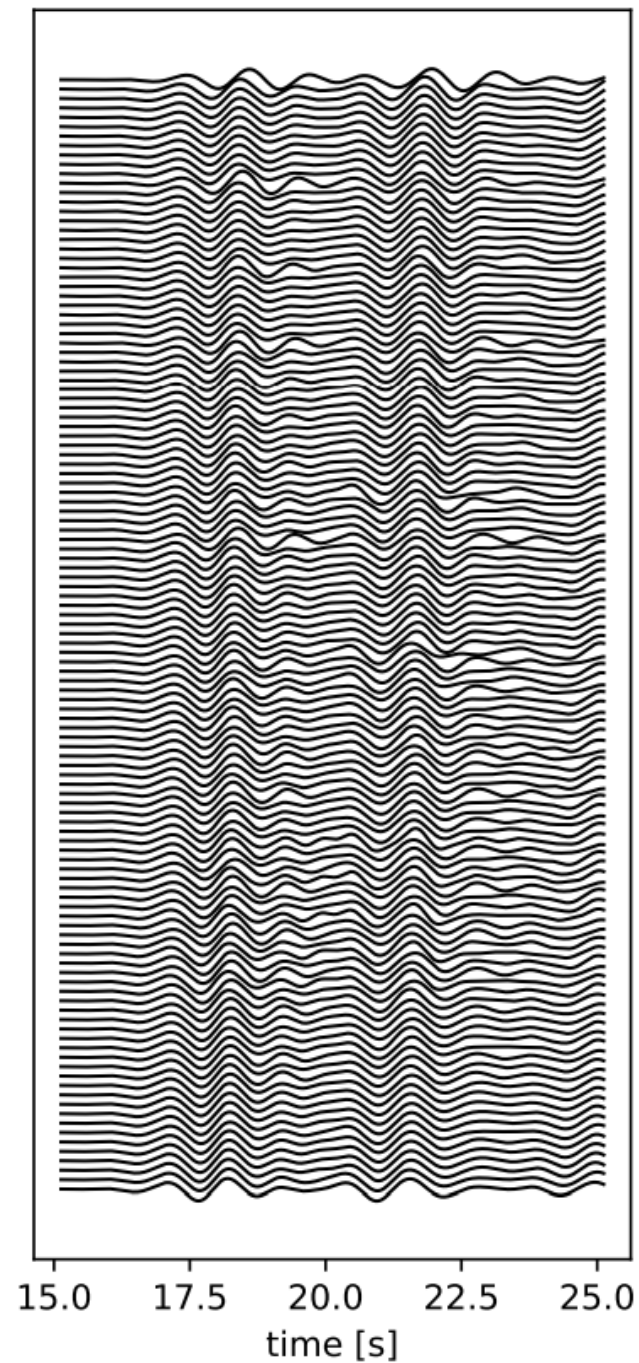
1-2 Hz



2-3 Hz



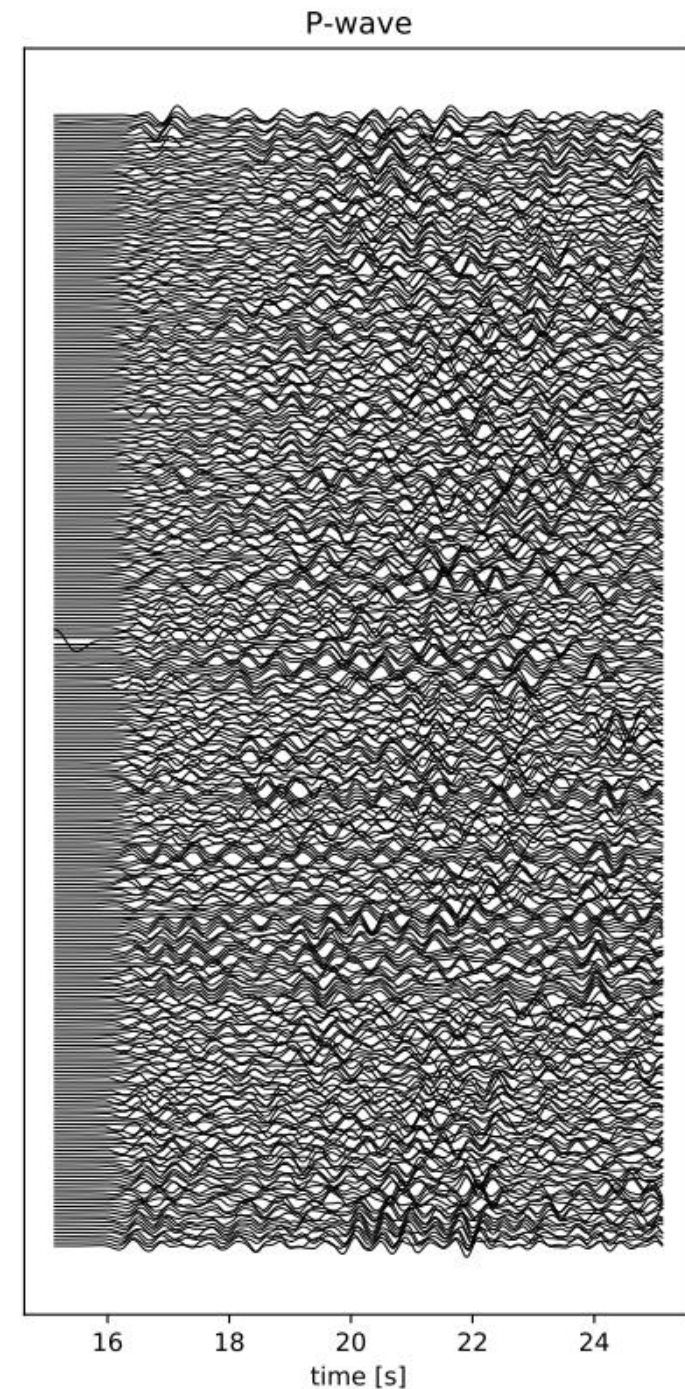
Z-component



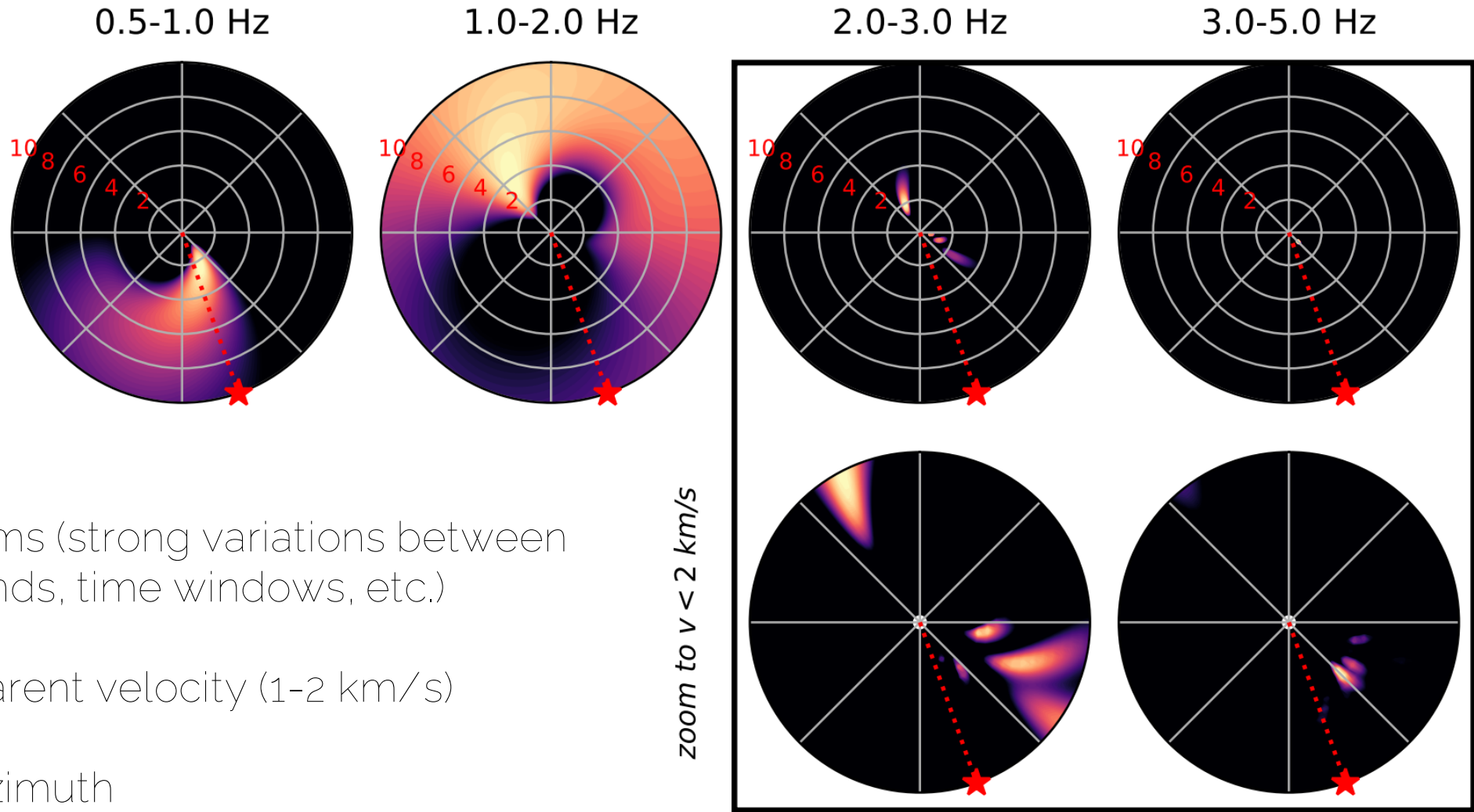
Apparent wave speed: 5 km/s Back-azimuth: SSE

DAS beamforming

- Poor waveform coherence P- and S-phases
- Some local waveform coherence in individual segments, but not at array-scale
- Good SNR \neq good coherence



DAS beamforming



Unstable beams (strong variations between frequency bands, time windows, etc.)

Very low apparent velocity (1-2 km/s)

Ambiguous azimuth

DAS vs. nodal array beamforming

- DAS array beamforming gives **very different results** than for the nodal array beamforming. Why?
- If the signal sources sensed by the DAS array are real, then **what do we measure?** (*what's that wiggle?*)

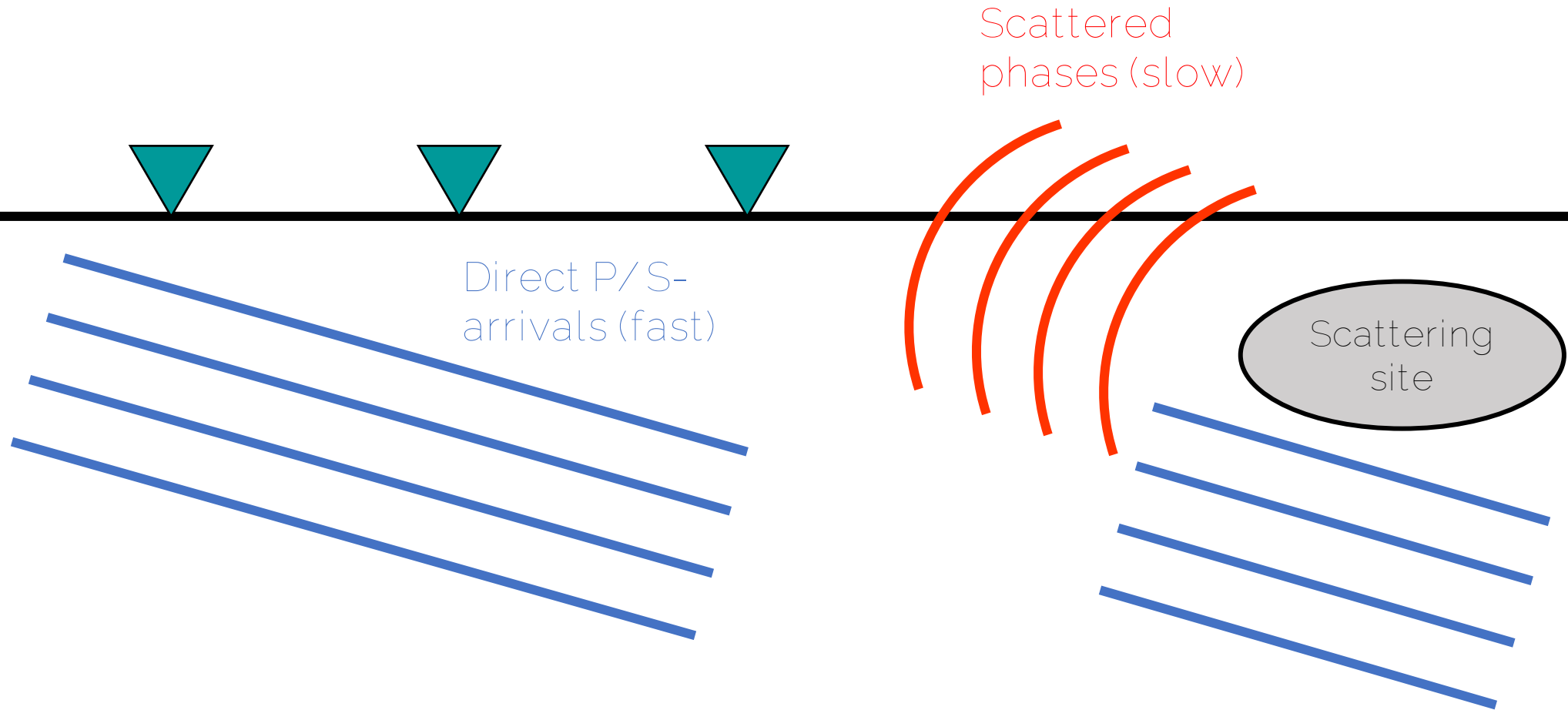
DAS slowness sensitivity

- Strain amplitudes are inversely proportional to phase velocity:

$$\varepsilon \equiv \frac{\partial u}{\partial x} = \pm \frac{\partial t}{\partial x} \frac{\partial u}{\partial t} = \pm \frac{1}{c} \dot{u}$$

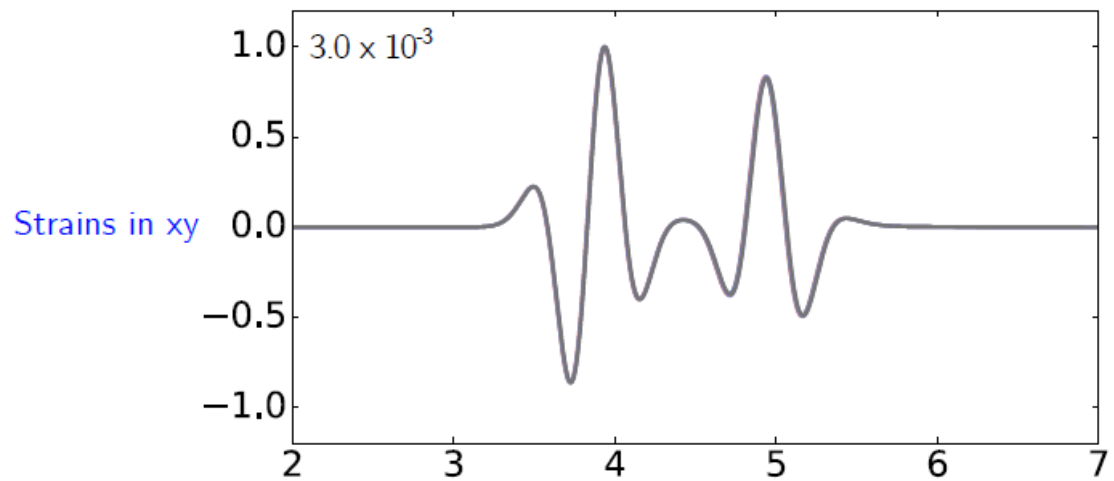
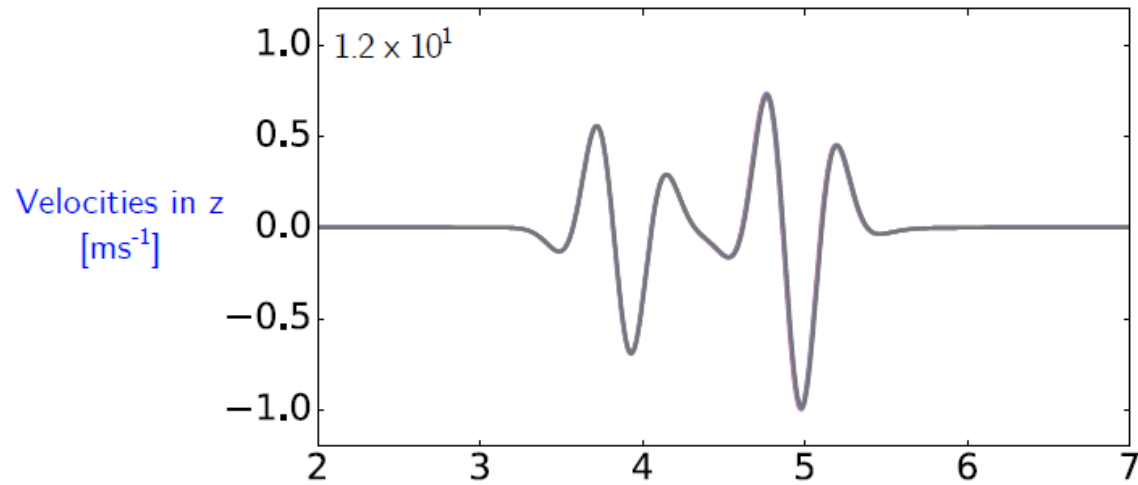
- Only horizontal components of strain are measured: highest signal amplitudes for apparently slow phases (e.g. shallow sources)

DAS slowness sensitivity



Phase velocity heterogeneities (Singh et al., 2020)

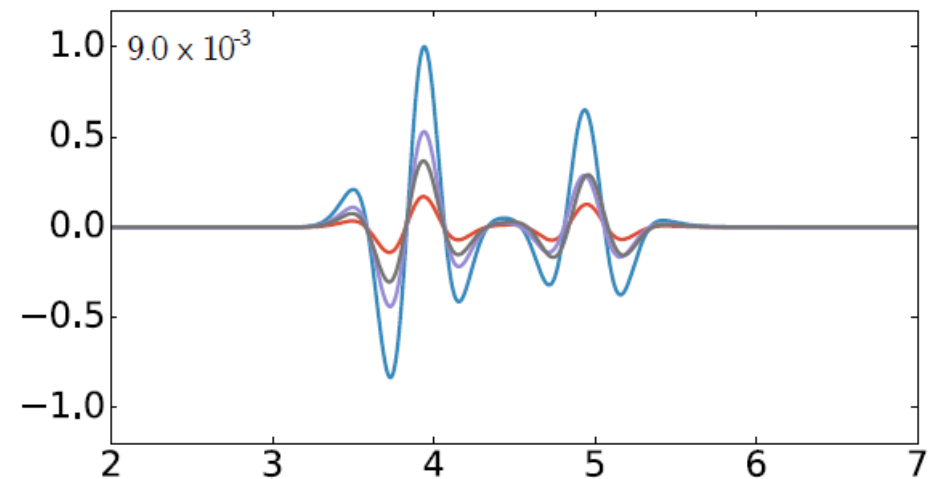
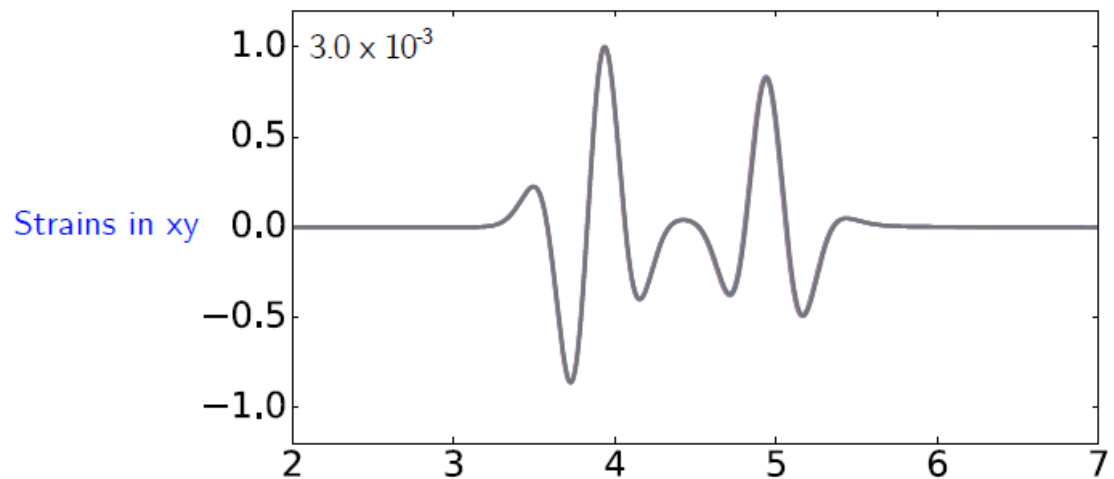
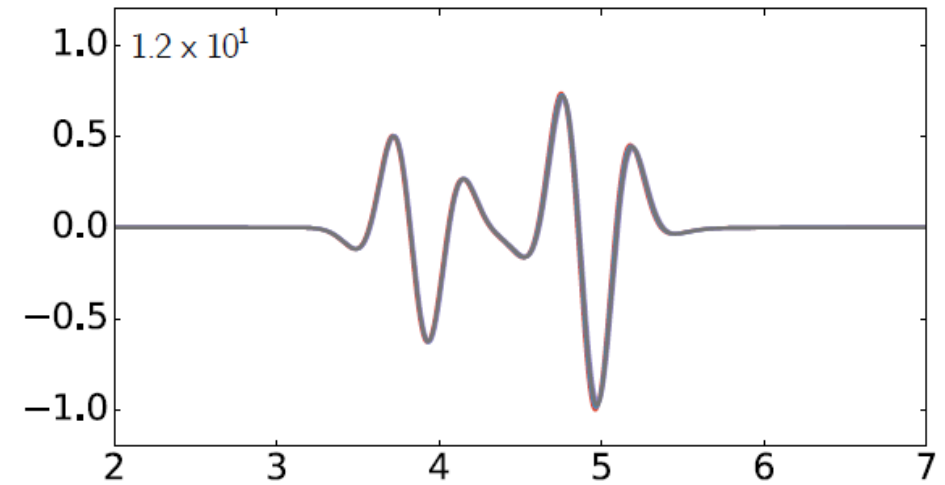
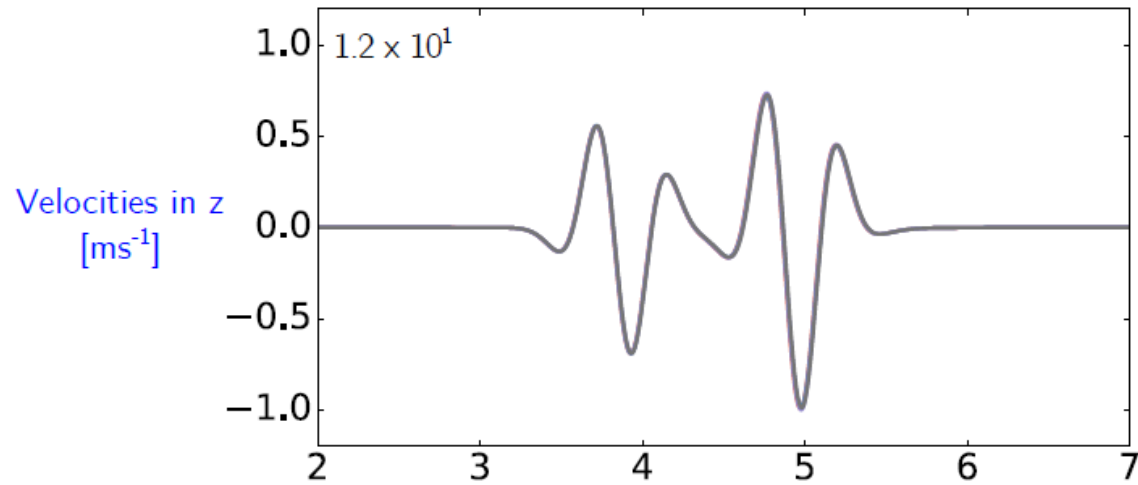
Homogeneous



Phase velocity heterogeneities (Singh et al., 2020)

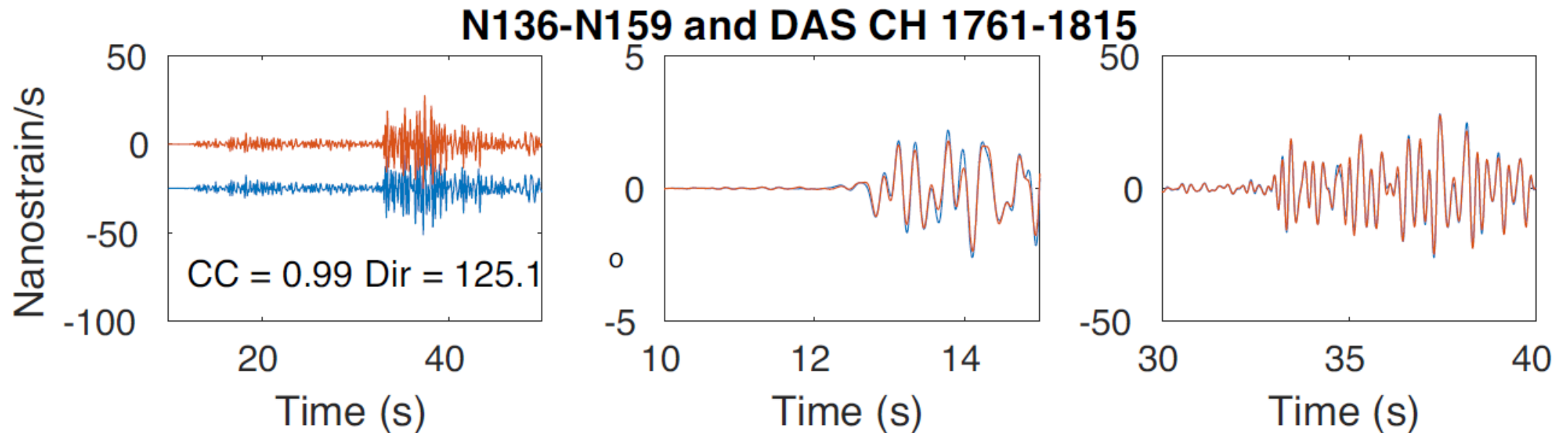
Homogeneous

Heterogeneous

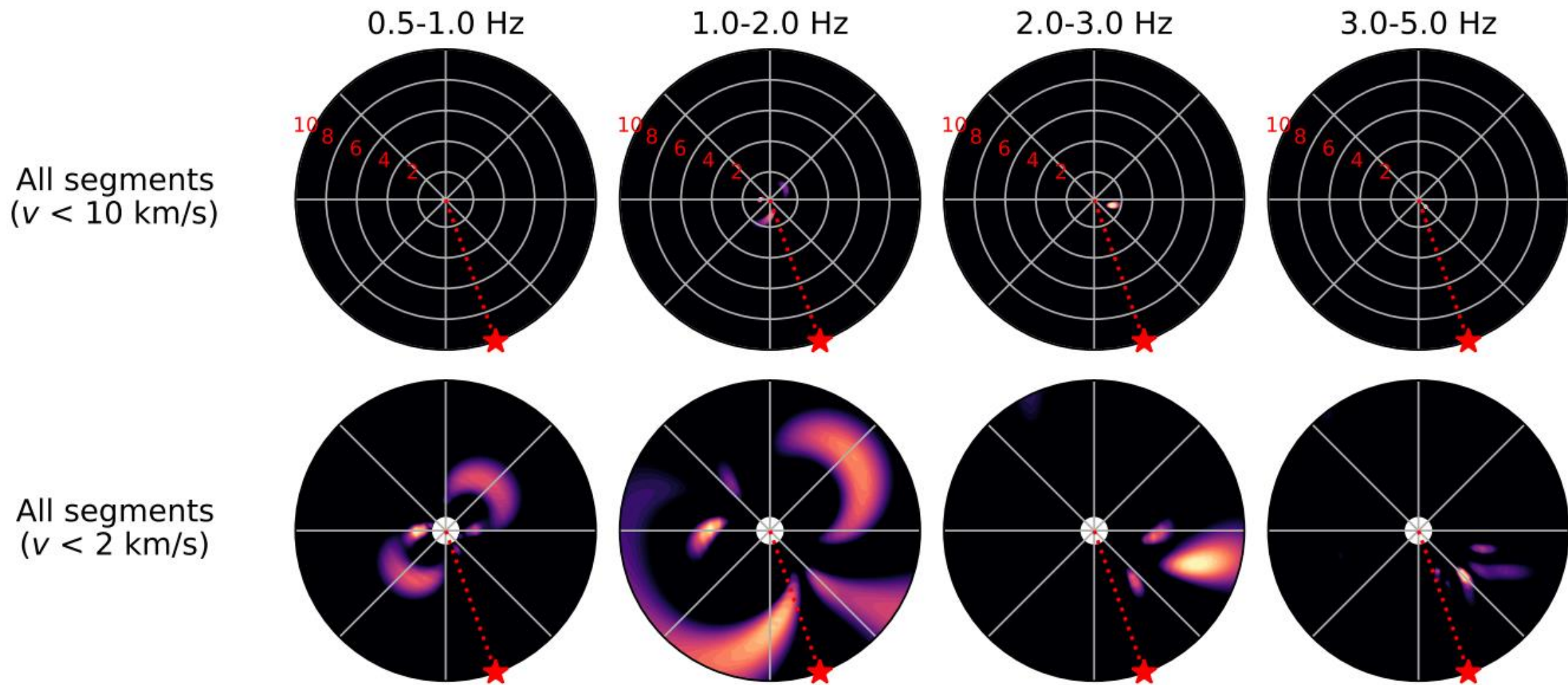


Testing hetero-sensitivity

- Wang et al. (2018): DAS waveforms can be reproduced wiggle-by-wiggle with a **finite-difference stencil**
- Take difference between particle velocity waveforms, divide by distance -> average strain rate between nodes



Virtual DAS beamforming



Solution: integrate DAS data

- Beamforming of particle velocities: excellent results
- Beamforming of strain rates: poor results
- Strain rate can be computed from particle velocities -> can we go the other way around?
- Experiment: integrating DAS strain rates along the fibre

$$\dot{u}(x_0 + L) = \dot{u}(x_0) + \int_{x_0}^{x_0+L} \dot{\epsilon}(x') dx' = \dot{u}(x_0) + L \dot{\epsilon}_{DAS}$$

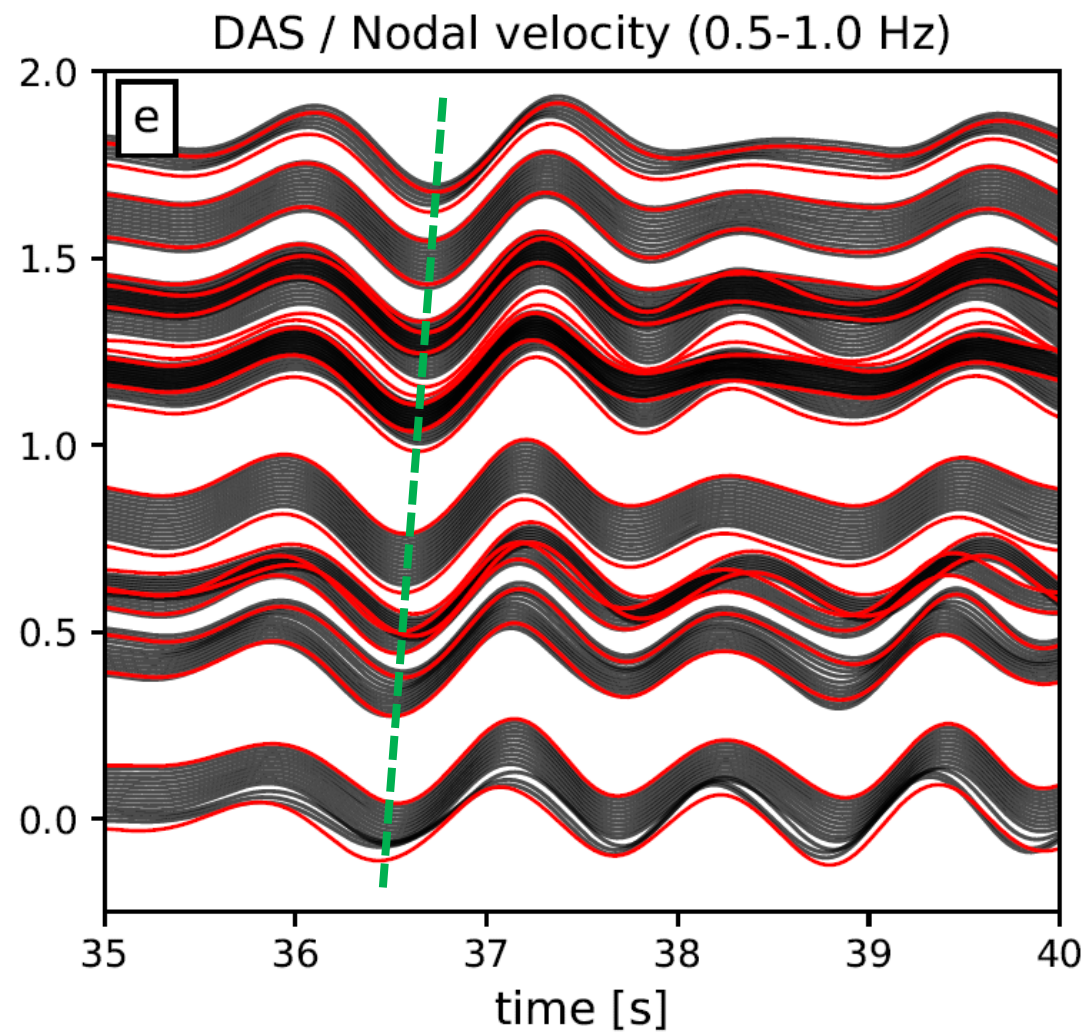
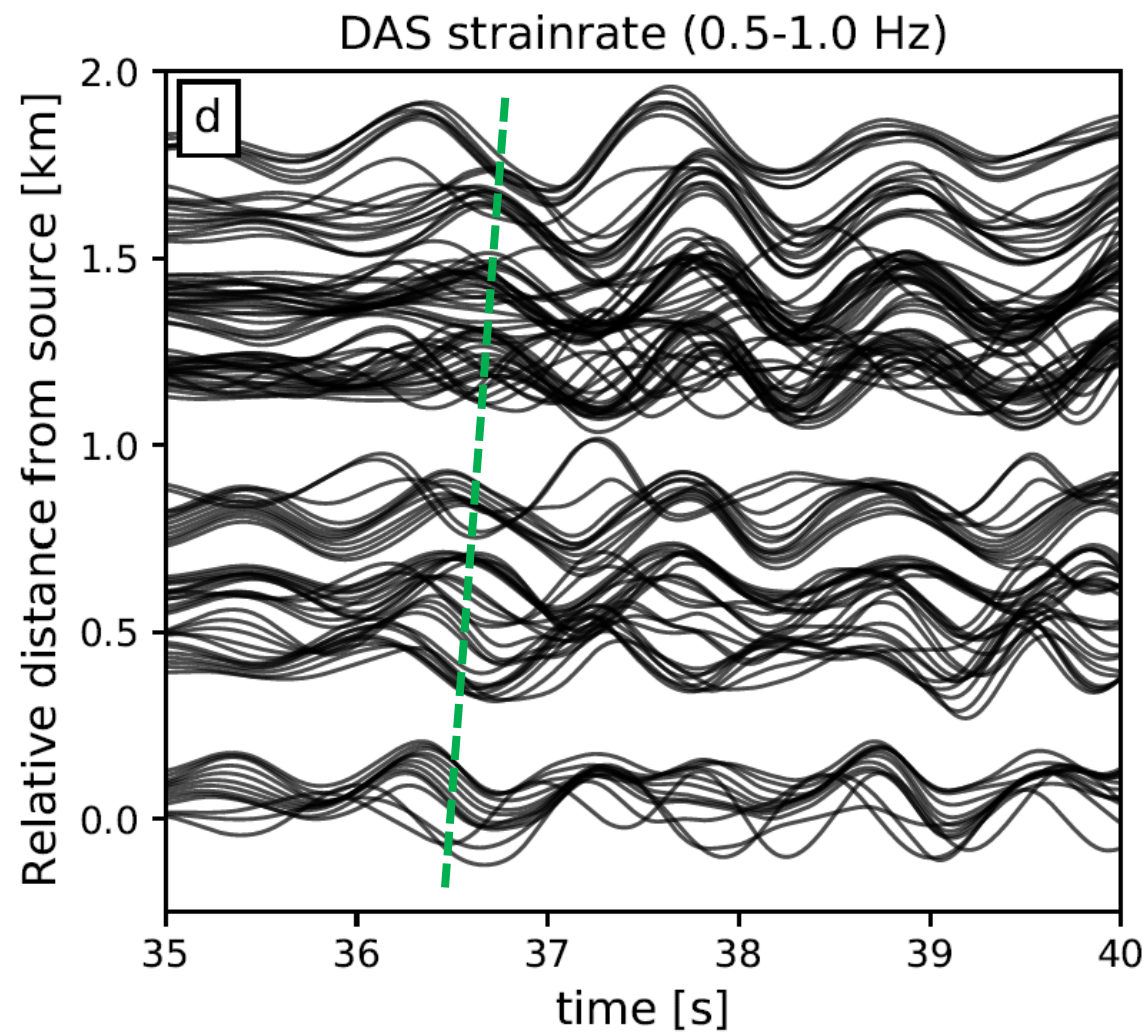
Solution: integrate DAS data

- For n DAS channels:

$$\dot{u}(x_0 + nL) = \dot{u}(x_0) + L \sum_{i=1}^n \dot{\epsilon}_{DAS,i}$$

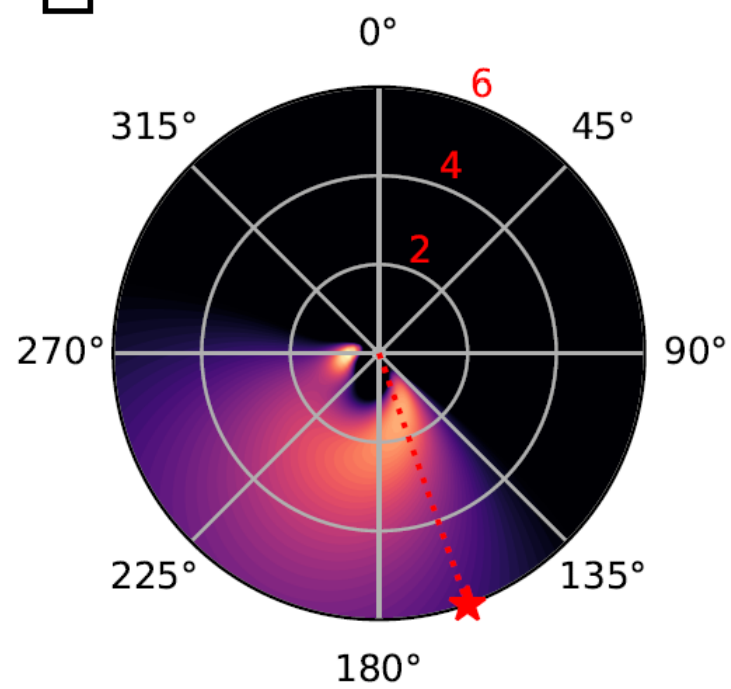
Requirements:

1. Straight DAS segments
2. Uniform coupling
3. One seismometer per segment

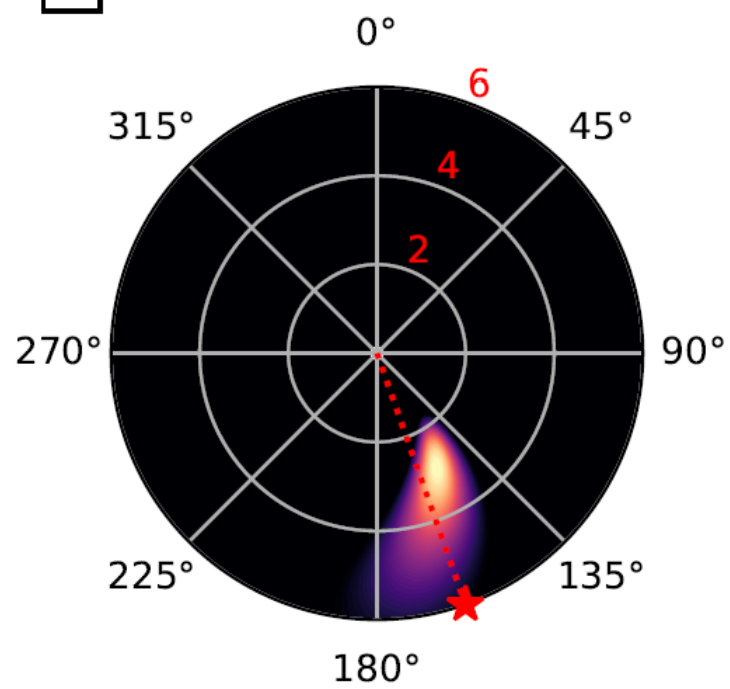


f

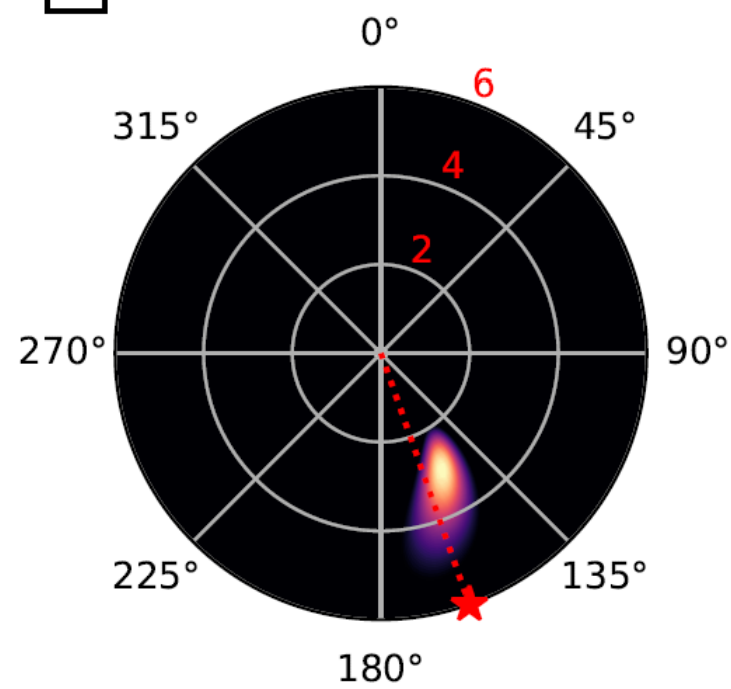
DAS strain rate

**g**

DAS integrated

**h**

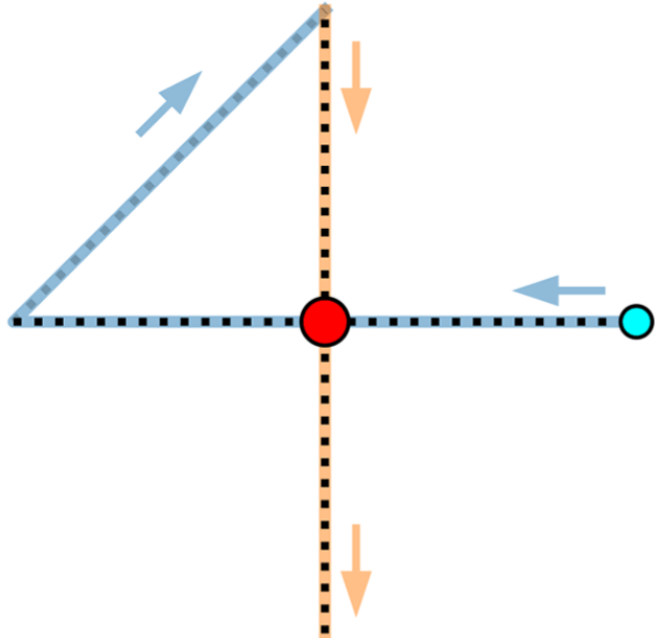
Nodal array



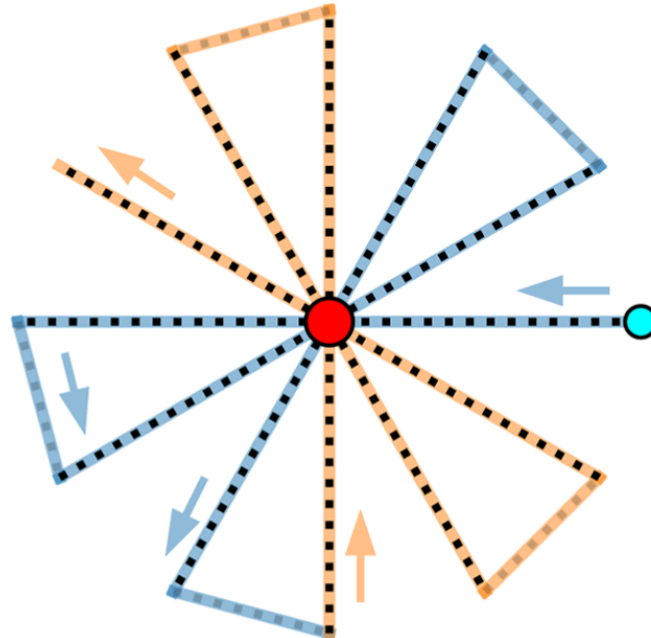
Hybrid array design



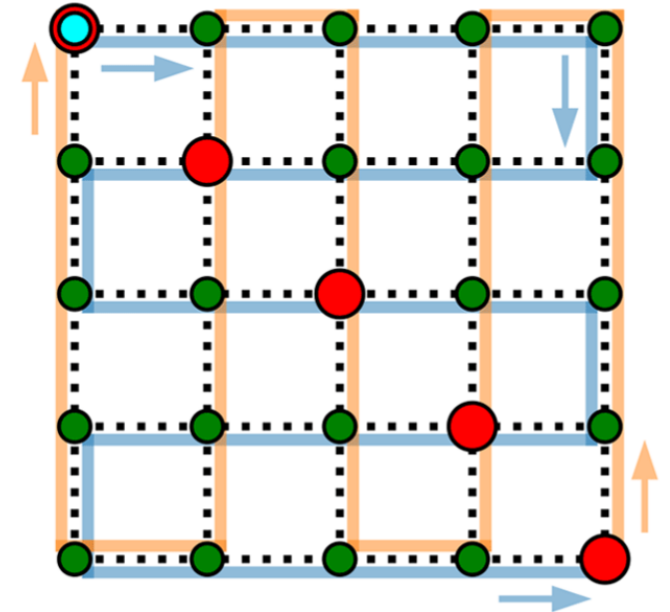
(a) 4-shape array



(b) Umbrella array



(c) Checkerboard array

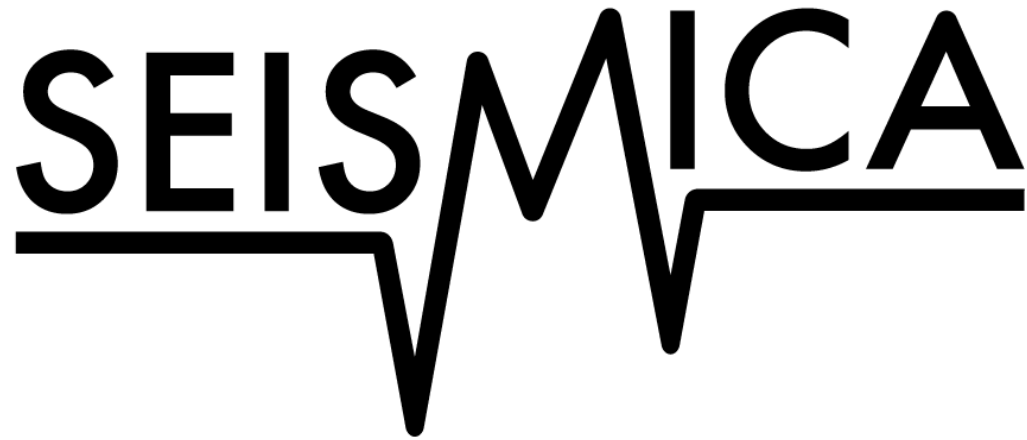


Take-home messages

1. The measurement principle of DAS (strain/strain rate) highlights local scattering and is very sensitive to heterogeneities
2. Strain (rate) measurements are less coherent, and so DAS is not a good substitute for conventional seismometer arrays in terms of beamforming, template matching, etc.
3. By integrating the DAS strain (rate) using a seismometer as a reference, all of the issues can be resolved
4. To get the best of both worlds, we need to deploy hybrid seismometer-DAS arrays

Support Open Science!

SEISMICA



Diamond Open Access journal for
seismological research

Free to publish, free to read, peer-reviewed

Expected launch: [January 2022](#)

Join us on Slack!

Email: info@seismica.org

Twitter: [@WeAreSeismica](#)

Data & Code



martijn.vandenende@oca.eu



[@martijnende](https://twitter.com/martijnende)

Published  at *Solid Earth*:

van den Ende & Ampuero (2021), *Solid Earth* 12

<https://doi.org/10.5194/se-12-915-2021>

Data & code available at *FigShare*:

<https://doi.org/10.6084/m9.figshare.12899288>